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## Tailoring superelasticity of soft magnetic materials

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Embedding magnetic colloidal particles in an elastic polymer matrix leads to smart soft materials that can reversibly be addressed from outside by external magnetic fields. We discover a pronounced nonlinear superelastic stress-strain behavior of such materials using numerical simulations. This behavior results from a combination of two stress-induced mechanisms: a detachment mechanism of embedded particle aggregates and a reorientation mechanism of magnetic moments. The superelastic regime can be reversibly tuned or even be switched on and off by external magnetic fields and thus be tailored during operation. Similarities to the superelastic behavior of shape-memory alloys suggest analogous applications, with the additional benefit of reversible switchability and a higher biocompatibility of soft materials. © 2015 AIP Publishing LLC.  
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The term “superelasticity” expresses the capability of certain materials to perform huge elastic deformations that are completely reversible.<sup>1,2</sup> Initially, it was introduced in the context of shape-memory alloys.<sup>3–5</sup> These metallic materials can perform large recoverable deformations due to stress-induced phase transitions. A transition to a more elongated lattice structure accommodates an externally imposed extension. Typically, this transition shows up as a pronounced “plateau-like” regime on the corresponding stress-strain curve. On this plateau, the samples are heterogeneous with domains of already transitioned material. Then, only relatively small additional stress induces a huge additional deformation. Smart material properties are observed:<sup>6–9</sup> upon stress release, shape-memory alloys can reversibly return to their initial state. They self-reliantly adapt their appearance to changed environmental conditions.

In the present letter, we demonstrate that an analogous phenomenological behavior can be realized for a very different class of materials, exploiting different underlying mechanisms. Moreover, we show that during operation the behavior can be reversibly tailored from outside by external magnetic fields. All of these are achieved by employing soft magnetic gels as working materials: colloidal magnetic particles embedded in a possibly swollen elastic polymer matrix.<sup>10</sup> Similar to magnetic fluids,<sup>11–18</sup> magnetic gels allow to reversibly adjust their material properties by external magnetic fields. In this way, switching the elastic properties<sup>19–23</sup> offers a route to construct readily tunable dampers<sup>24</sup> or vibration absorbers,<sup>25</sup> while the possibility to switch the shape<sup>19,26–28</sup> allows application as soft actuators.<sup>29–31</sup>

Here, we show that magnetic gels due to the interplay between magnetic and elastic interactions likewise feature superelastic behavior: it is enabled by a detachment mechanism of embedded magnetic particle aggregates and by a reorientation mechanism of magnetic moments. Both mechanisms are stress-induced and respond to external magnetic fields.

Therefore, superelasticity can be switched on and off, and also its magnitude and position on the stress-strain curve can be reversibly tailored during operation, as has been realized for some special metallic components.<sup>32,33</sup> The superelastic behavior in our case covers a significantly larger strain regime. Furthermore, soft gel-like materials generally provide a larger deformability and higher degree of biocompatibility<sup>34–38</sup> than metallic alloys. This becomes particularly important for medical applications.<sup>39</sup> There has been a significant effort to transfer the properties of shape-memory alloys to soft materials.<sup>35,37,38,40</sup> Here, we report on reversibly tailoring superelastic properties by external magnetic fields.

We concentrate on anisotropic uniaxial magnetic gels.<sup>19,22,41,42</sup> They are manufactured by applying a strong external magnetic field during preparation, which leads to the formation of oriented straight chain-like aggregates of embedded magnetic particles.<sup>43–46</sup> After subsequent chemical cross-linking of the embedding polymer network, the position of the particles gets permanently locked.<sup>47</sup> We assume that the magnetic moments carried by the particles are free to reorient. First, for diameters up to 10–15 nm, this applies within the interior of each magnetic particle.<sup>48</sup> Second, this is possible when each particle as a whole is free to rotate,<sup>47</sup> e.g., when the polymer is not completely cross-linked in the immediate particle vicinity.<sup>49</sup> Another example is yolk-shell particles with a magnetic core that can rotate within the shell.<sup>50,51</sup> If reorientations of the magnetic moments are blocked, only the first of the two mechanisms described below is active.

We identify a superelastic stress-strain behavior of uniaxial magnetic gels by numerically investigating the following model system. Identical spherical colloidal particles, each carrying a permanent magnetic dipole moment, are embedded in a continuous elastic matrix. The elastic deformation energy of the matrix is described by a standard nearly incompressible Neo-Hookean model.<sup>52,53</sup> We tessellate the matrix into sufficiently small tetrahedra by Delaunay triangulation.<sup>54</sup> Each tetrahedron may deform affinely, increasing its elastic energy, from which we extract restoring forces on

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its delimiting nodes. The nodes attached to surfaces of rigid embedded particles transmit forces and torques to these particles. Energy minimization with respect to all nodes and particle positions, as well as all particle and dipole orientations, is performed (see supplementary material for technical details<sup>53</sup>).

Within our model, we study small three-dimensional systems, each containing 96 magnetic particles (Fig. 1(a)). For initialization, we arrange the particles in straight linear chain-like aggregates: each chain is one particle in diameter but several equi-distanced particles in length that are separated by finite gaps filled with elastic material.<sup>22,49,55–57</sup> Initially, the chains are aligned parallel to each other, but otherwise placed in a random non-overlapping way.<sup>53</sup> In the

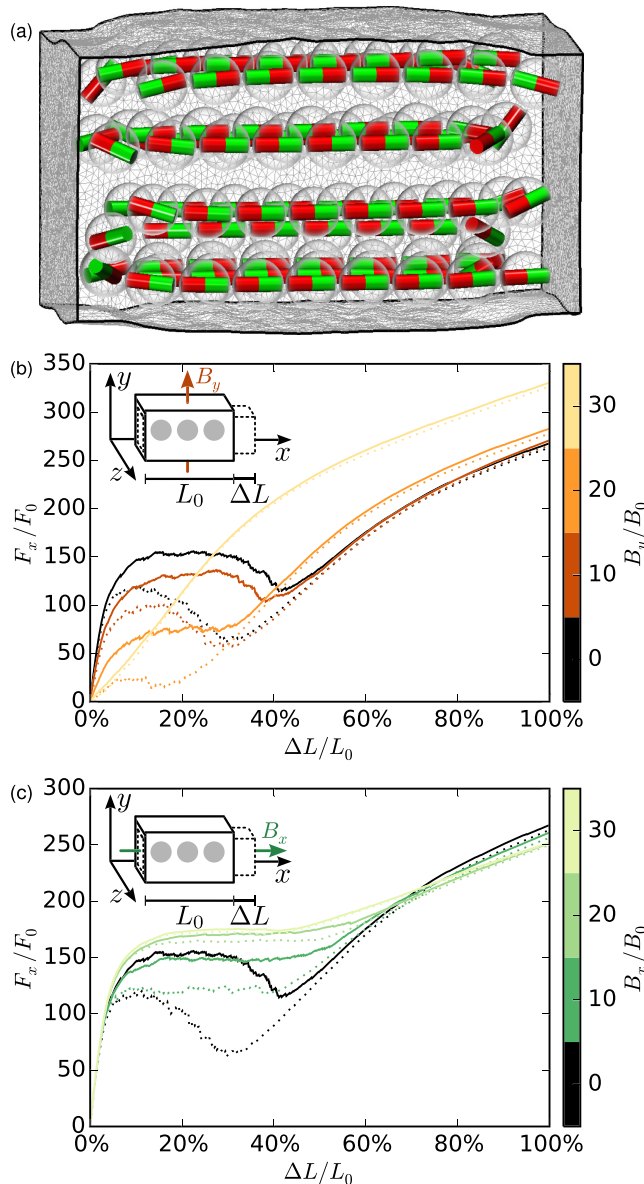


FIG. 1. (a) A snapshot of an equilibrated system of chain-like aggregates before stretching. The small bar magnets in the embedded particles indicate dipole moments. (b) Uniaxial stress-strain behavior for stretching in chain direction, revealing a pronounced superelastic plateau-like nonlinearity, and adjustability by magnetic fields perpendicular to the chains. (c) Effects of magnetic fields parallel to the chains. As in all subsequent figures, the solid lines represent loading and the dotted lines unloading, highlighting reversibility.

presence of the rigid inclusions, the elastic modulus increases<sup>53</sup> by a factor of  $\sim 7$ . Finally, the magnetic moments are switched on, and the system is equilibrated, leading to an initial matrix deformation (Fig. 1(a)).

We quasistatically stretch our systems along the chain direction. To impose a certain extension, the mesh nodes at two opposite system boundaries are displaced into opposite directions in small steps. After equilibration during each step, the forces on the boundary nodes are measured. We check the reversibility of the induced total deformations by repeated loading and unloading cycles. Forces  $F$  are measured in units of  $F_0 = ER^2$ , magnetic fields  $B$  in units of  $B_0 = \sqrt{\frac{\mu_0}{4\pi}}E$ , and magnetic dipole moments  $m$  in units of  $m_0 = R^3 \sqrt{\frac{4\pi}{\mu_0}}E$ . Here,  $E$  is the elastic modulus of the matrix,  $R$  the particle radius, and  $\mu_0$  the vacuum permeability.  $L_0$  denotes the initial total length in stretching direction,  $\Delta L$  is the (absolute) elongation, and  $\Delta L/L_0$  is the elongational strain. We fix the material parameters by setting the Poisson ratio of the matrix to  $\nu = 0.495$  and the magnetic moment to  $m = 10 m_0$ .

Figs. 1(b) and 1(c) illustrate the resulting markedly non-linear stress-strain behavior. First, the force to achieve a certain elongation steeply increases with the imposed strain. Then, a pronounced superelastic nonlinearity follows. Since our measurements are strain-controlled, and due to the finite size of our systems, we observe a regime of negative slope. A macroscopic sample in this region would become inhomogeneous, leading to a plateau-like superelastic regime<sup>4,6</sup> or likewise show a negative slope under strain control.<sup>58</sup> In this area, a further slight increase in the applied force induces a huge additional deformation. Remarkably, we can reversibly shift the non-linearity to smaller strains by a perpendicular external magnetic field (Fig. 1(b)). High field strengths even switch off the non-linearity. Furthermore, we can alter the shape of the plateau-like regime by a field in stretching direction (Fig. 1(c)). At the end of the plateau, the stress-strain curve crosses over to a relatively constant intermediate slope.

We found that a combination of two effects allows for this adjustable superelastic behavior: a stress-induced detachment mechanism of the individual chain-like aggregates (Fig. 2) plus a reorientation mechanism of the magnetic moments (Figs. 3 and 4). To illustrate the first one, Fig. 2(a) shows the initialized state of an example chain system. Switching on magnetic interactions, the particles attract each other and “pre-compress” the elastic gap material (Fig. 2(b)). Now the particles are located at a small distance from each other, its inverse cube setting the dipolar interaction scale. The initial steep increase in the stress-strain curve (Fig. 2(f)) reflects these strong magnetic interactions. Once the magnetic barrier is overcome, a small further increase in the stretching force is sufficient to detach part of the chain from the remainder (Fig. 2(c)). Such events suddenly elongate the system and lead to spikes in the stress-strain curve (Fig. 2(f)). They repeatedly occur (Fig. 2(d)) until all particles have been detached from each other. In total, a spiky plateau appears (Fig. 2(f)). It smoothens when averaged over different chains (Fig. 1). This is an intra-chain effect. Inter-chain

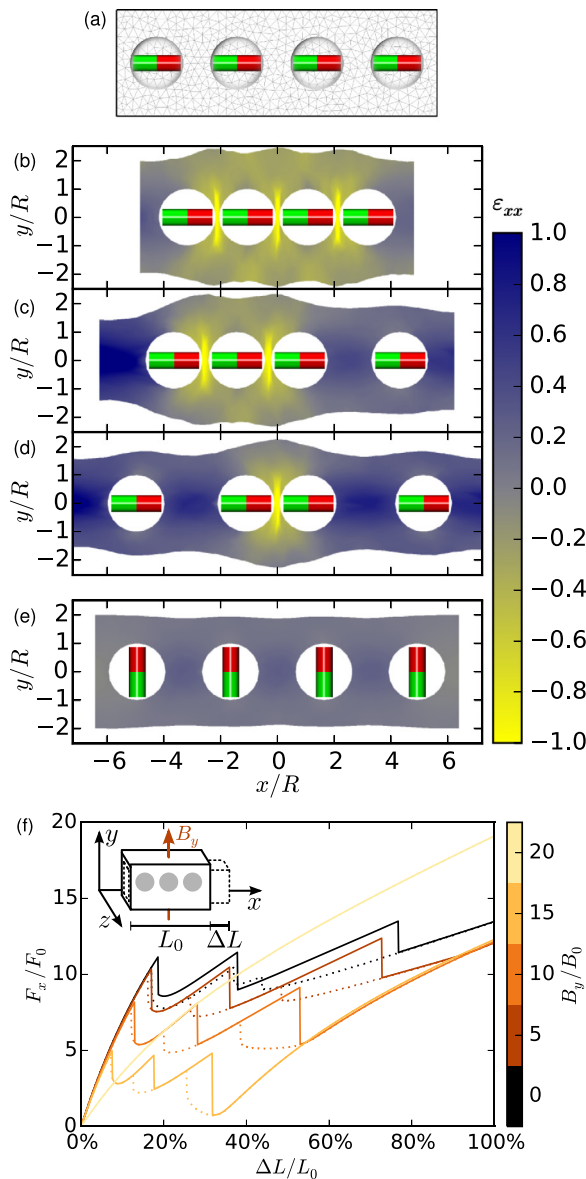


FIG. 2. Illustration of the detachment mechanism: (a) A cut through an initialized four-particle single-chain system: the elastic matrix is not yet deformed. (b) Equilibrated state with the pre-compressed gap material. The color maps show the local matrix distortion along the longitudinal stretching direction, here illustrated using the so-called “true strain”  $\epsilon_{xx}$ .<sup>59</sup> (c) First and (d) second detachment events of parts of the chain where magnetic energy barriers are overcome by longitudinally applied stretching forces. (e) The equilibrated unloaded state in the presence of a strong perpendicular magnetic field. All magnetic moments are realigned; thus, there is no pre-compression and no magnetic energy barrier. (f) Stress-strain curves for various perpendicular field strengths. Each spike corresponds to a detachment event where a magnetic energy barrier is overcome. An increasing perpendicular magnetic field lowers the detachment threshold, until superelasticity is switched off.

interactions are minor for experimentally reported particle fractions.<sup>22,60</sup> Thus, the finite size of our model systems will not affect the significance of the overall material behavior.

Now, the tunability by a perpendicular magnetic field becomes clear (Figs. 2(e) and 2(f)). Strong perpendicular fields align all dipoles in the perpendicular direction. There is no pre-compression (Fig. 2(e)); hence, no magnetic energy barrier for pulling the particles apart, and thus, no corresponding stress-strain nonlinearity. Smaller magnetic fields do not significantly alter the dipole orientations in the pre-

compressed state due to the strong magnetic interactions at short distances. Yet, they affect the threshold for detachment (Fig. 2(f)); the moments can rotate away from the chain axes when the particle separation increases.

The second effect contributing to the superelastic nonlinearity results from the stretching-induced reorientations of the magnetic dipole moments. For illustration, we explain it on a regular cuboid lattice arrangement (Fig. 3). Initially, the edges of the cuboid unit cells are shorter along the stretching direction (Fig. 3(a)). Thus, the dipoles align parallel to it. During elongation (Fig. 3(b)), these distances increase. Simultaneously, due to the overall volume preservation, the system contracts from the sides. This decreases the separation perpendicular to the stretching direction. When the edge lengths of the distorted unit cells become equal in both directions, there is no single favored dipole orientation left (Fig. 3(b)). Further stretching makes the dipoles rotate into the plane perpendicular to elongation (Fig. 3(c)). Thus, during the overall process, the magnetic dipoles reorient (“flip”). This flipping effect is sensitive to the spatial particle arrangement. Yet, it likewise appeared in all of our investigated uniaxial systems. It is obvious from Fig. 3(b) that we can identify the flipping effect by a vanishing orientational order of the magnetic moments (see supplementary material for a quantitative evaluation<sup>53</sup>). A similar orientational analysis for the separation vectors between all nearest-neighbor particles demonstrates that the mechanism is indeed triggered by the changes in the distances mentioned above.<sup>53</sup>

The flipping process is reflected by a steep step in the corresponding stress-strain curve (Fig. 4; see supplementary material for a simplified energetic model, including larger system sizes<sup>53</sup>). Also, this flipping contribution to the superelastic stress-strain behavior can be tuned from outside. Through a perpendicular magnetic field, flipping can be shifted to lower strains or be switched off completely, which largely eliminates the corresponding nonlinearity in the stress-strain curve (Fig. 4(a)). However, also a parallel field has a significant influence: it can postpone flipping to larger deformations and smear out the connected stress-strain nonlinearity (Fig. 4(b)). In Fig. 1(c), it is the dip in the stress-strain curve that is mainly connected to the flipping mechanism and can be switched off by the parallel field. The step jumps of Fig. 4 appear more rounded in Figs. 1(b) and 1(c) because all stress-strain curves in Fig. 1 were obtained by averaging over twenty characteristic numerical realizations. For larger system sizes, the curves would appear still more rounded.

To amplify the effects and to realize our assumed value of  $m = 10m_0$ , strong magnetic moments and soft elastic matrices are preferred. A possible route is to use particles made of a material of high remanent magnetization, for example, NdFeB<sup>61</sup> (more than  $2 \times 10^5$  A/m). Soft elastic matrices of  $E \leq 10^3$  Pa can be made of silicone<sup>23,62,63</sup> or polydimethylsiloxane.<sup>64</sup> The problem is qualitatively invariant under rescaling all lengths by a characteristic dimension such as the particle radius  $R$ . Thus, the particle size is not a critical factor. Our calculations were performed for permanent reorientable magnetic moments. Yet, the reorientation effect could likewise be observed using soft magnetic particles that are magnetized by an external magnetic field. Then, the reorientation

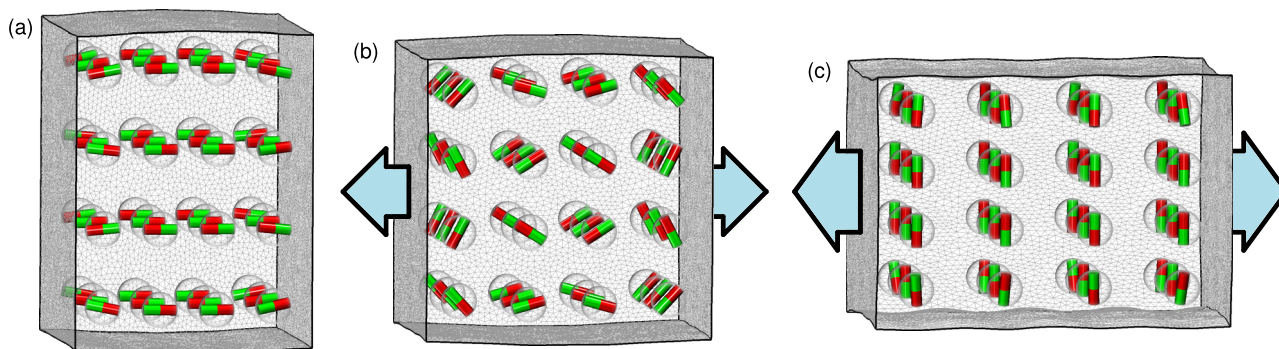


FIG. 3. An illustration of the reorientation mechanism: snapshots of a stretched regular cuboid-lattice system (here  $m = 8m_0$ ). (a) Initially, the particles are closest in stretching direction (horizontal), their magnetic moments aligning along this direction. Stretching the system increases the distances along and (due to volume preservation) decreases the distances perpendicular to the stretching direction. (b) When these distances become approximately equal, no particular orientation is preferred. (c) Stretching the system further makes a perpendicular direction the preferred one; the orientations of the magnetic moments “flip.”

process must be performed “manually” by switching the external magnetic field direction.

In conclusion, we have identified a superelastic stress-strain behavior of soft uniaxial magnetic gels. These materials consist of chain-like aggregates of magnetic colloidal particles embedded in a soft elastic polymer matrix. Stretching the systems in chain direction reveals a significant nonlinearity in the stress-strain curve. In this regime, the systems can be strongly deformed with hardly any additional load necessary. Two underlying stress-induced mechanisms were identified: a detachment mechanism of the embedded

chain-like aggregates and a reorientation mechanism of the magnetic moments. Both the processes are reversible upon stress release, in analogy to the superelastic behavior of shape-memory alloys. As an additional benefit, the superelastic properties in the present case can be reversibly switched during operation by an external magnetic field.

These nonlinear stress-strain properties open the pathway to numerous applications. The on-demand tunable deformability could be used for easily applicable packaging or gaskets that become rigid when an external magnetic field is switched off. Under pre-stress, external magnetic fields can trigger significant deformations, qualifying the materials for the use as soft actuators. Combined with an increased biocompatibility, these concepts should be transferable to medical applications such as quick wound dressings, artificial muscles, or tunable implants. Finally, combinations of magnetic gels with other materials can bestow the tunable superelastic properties on the resulting composite.

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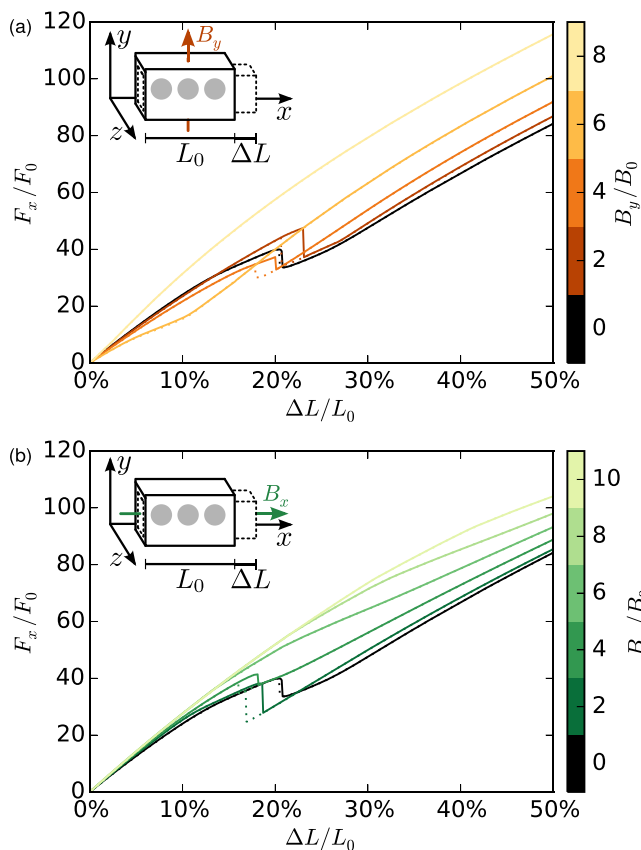


FIG. 4. Stress-strain curves of the cuboid-lattice system showing a steep drop as reorientation (flipping) occurs. (a) Perpendicular external magnetic fields shift this feature to lower strains, while (b) parallel external magnetic fields smear out the nonlinearity and postpone flipping to higher strains.

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